

$$1 - \underbrace{\binom{10}{9}}_{10} \cdot \left(\frac{8}{36}\right)^9 \left(\frac{28}{36}\right)^{10-9} - \underbrace{\binom{10}{10}}_1 \cdot \left(\frac{8}{36}\right)^{10} \left(\frac{28}{36}\right)^{10-10} = \boxed{1 - 10 \cdot \left(\frac{8}{36}\right)^9 \cdot \left(\frac{28}{36}\right) - \left(\frac{8}{36}\right)^{10}}$$

$$= \boxed{\text{Some \#}}$$

HW 6

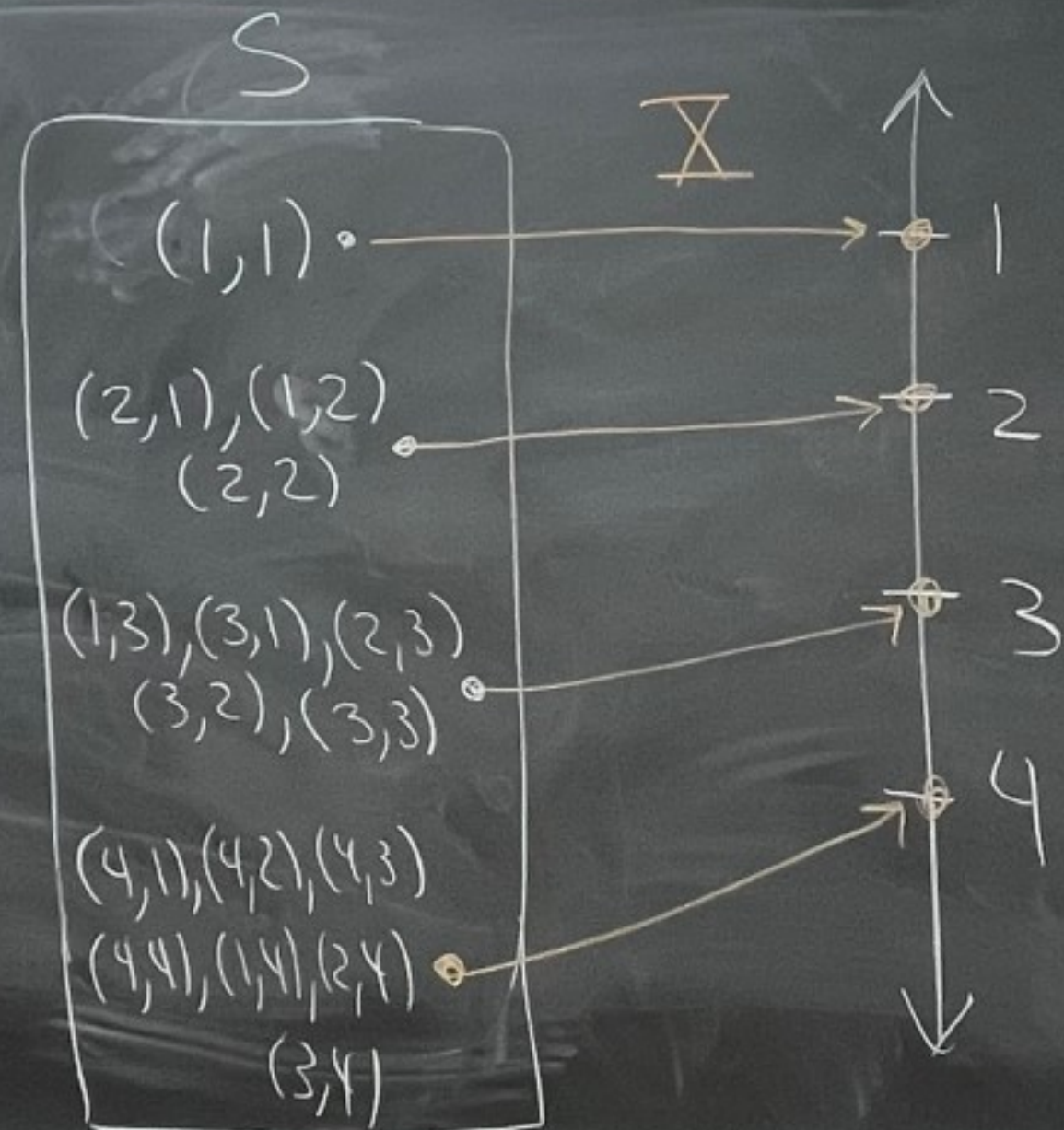
(3) roll two 4-sided dice
 X = maximum of dice

(a) draw X and p

(b) calculate F

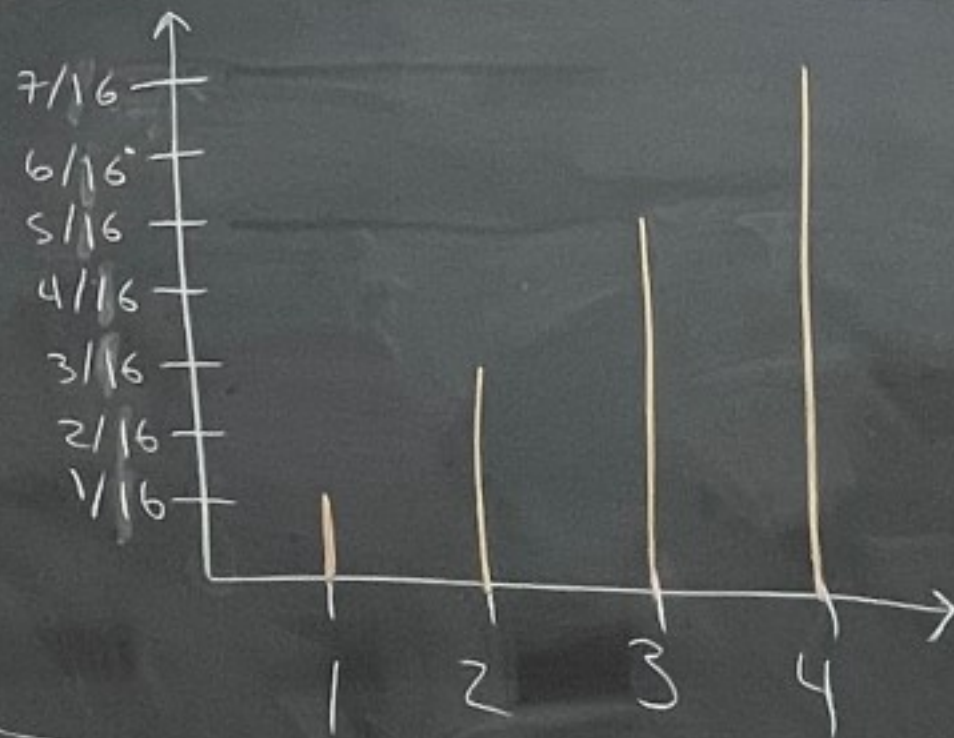
(c) Calculate $E(X)$, $\text{Var}(X)$, σ .

(a)



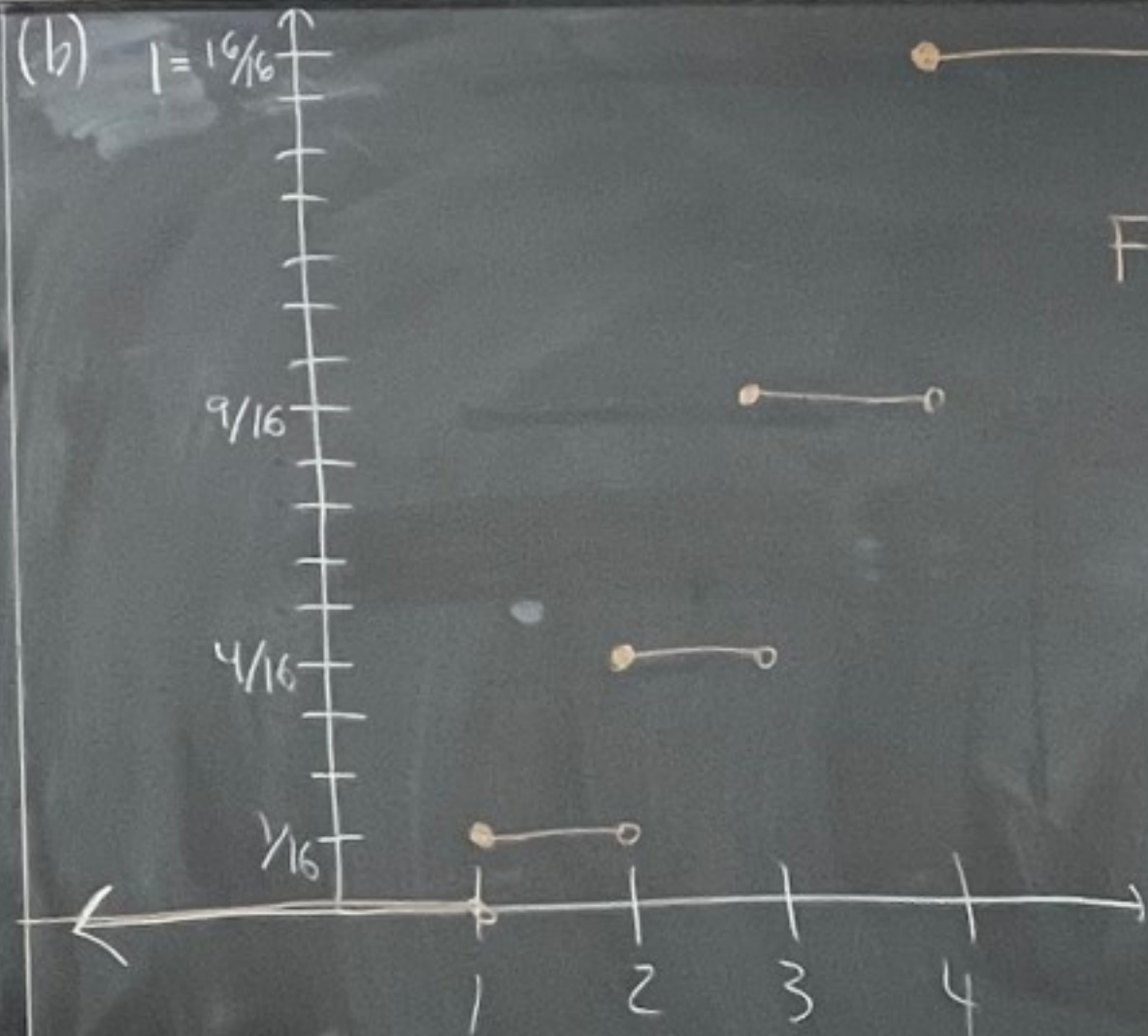
$$P(\bar{X}=1) = 1/16$$
$$P(\bar{X}=2) = 3/16$$

$$P(\bar{X}=3) = 5/16$$
$$P(\bar{X}=4) = 7/16$$



$$p(k) = P(\bar{X}=k)$$

(b) $1 = 16/16$



$$F(k) = P(X \leq k)$$

(c)

$$E[X] = (1)\left(\frac{1}{16}\right) + (2)\left(\frac{3}{16}\right) + (3)\left(\frac{5}{16}\right) + (4)\left(\frac{7}{16}\right) \\ = \boxed{50/16}$$

$$\text{Var}(X) = E[X^2] - [E[X]]^2$$

$$E[X^2] = (1)^2\left(\frac{1}{16}\right) + (2)^2\left(\frac{3}{16}\right) + (3)^2\left(\frac{5}{16}\right) + (4)^2\left(\frac{7}{16}\right) \\ = 170/16$$

$$\text{Var}(X) = \frac{170}{16} - \left(\frac{50}{16}\right)^2 = \boxed{\frac{220}{256}} = \boxed{\frac{55}{64}}$$

$$\sigma = \sqrt{\text{Var}(X)} = \boxed{\sqrt{\frac{55}{64}}}$$

$$\rightarrow E[\bar{X}] = np = 100 \left(\frac{7}{16}\right) = \frac{700}{16}$$

$$P(\bar{X}=21) = \binom{100}{21} \cdot \left(\frac{7}{16}\right)^{21} \cdot \left(\frac{9}{16}\right)^{100-21} = \frac{100!}{21!79!} \cdot \frac{7^{21}}{16^{21}} \cdot \frac{9^{79}}{16^{79}}$$

rolling two 4-sided dice 100 times
 \bar{X} = # times 4 occurs as one of the dice

$$p = \frac{7}{16} \rightarrow \text{success} = \{(1,4), (2,4), (3,4), (4,4), (4,1), (4,2), (4,3)\}$$

$$1-p = \frac{9}{16} \rightarrow \text{failure} = \{(1,2), (1,3), (2,1), (2,3), (3,1), (3,2), (3,3), (1,1), (2,2)\}$$

$$E[\bar{X}] = 0 \cdot P(\bar{X}=0) + 1 \cdot P(\bar{X}=1) + 2 \cdot P(\bar{X}=2) + \dots + 100 \cdot P(\bar{X}=100)$$

